

First, look for obvious simplifications.

Second, look for obvious substitutions.

Third, start looking for one of our four other methods:

*For Products, log's, inverse trig*

## **INTEGRATION BY PARTS**

$$u = \quad \quad dv =$$

$$du = \quad \quad v =$$

If you're stuck on choosing  $u$  remember LIPET.  
(But after you get comfortable with this method,  
you shouldn't need LIPET anymore)

*For sin's, cos's, tan's, sec's*

## **TRIG. INTEGRALS**

1. Odd cos  $\rightarrow u = \sin(x)$
2. Odd sin  $\rightarrow u = \cos(x)$
3. Even sec  $\rightarrow u = \tan(x)$
4. Odd tan  $\rightarrow u = \sec(x)$
5. Even sin & cos  $\rightarrow$  Half Angle Identities

In the first 4 cases you need the identities:

$$\sin^2(x) = 1 - \cos^2(x)$$

$$\cos^2(x) = 1 - \sin^2(x)$$

$$\tan^2(x) = \sec^2(x) - 1$$

$$\sec^2(x) = \tan^2(x) + 1$$

For the 5<sup>th</sup> case, you need the half angle identities:

$$\sin^2(x) = (1 - \cos(2x))/2$$

$$\cos^2(x) = (1 + \cos(2x))/2$$

$$\sin(x)\cos(x) = \sin(2x)/2$$

*For radicals with  $a^2 - x^2$ ,  $x^2 + a^2$ ,  $x^2 - a^2$  or if quadratic doesn't factor*

## **TRIG. SUBSTITUTION**

If the quadratic has a linear term ('middle term') and it doesn't factor, then you need to complete the square. (1/2 of middle term, square, add and subtract value) The rest of the method follows by making the correct substitution.

$$x = a \sin(\theta) \quad (\text{for } a^2 - x^2)$$

$$x = a \tan(\theta) \quad (\text{for } x^2 + a^2)$$

$$x = a \sec(\theta) \quad (\text{for } x^2 - a^2)$$

At the end, draw and label the TRIANGLE to get back to x's

*For rational functions*

## **PARTIAL FRACTIONS**

Divide if the power of top is bigger than power on bottom.

Then factor the bottom and set up and solve the partial fraction decomposition.

**Distinct Linear Factors**

→ Determine a constant for each factor.

**Non-Distinct Linear Factors**

→ Determine a constant for each factor, along with each power from 1 up to the number of times repeated.

**Irreducible Quadratic Factor**

→ Complete the square, the numerator of the factor is  $Ax+B$ .