

Math 124 H Autumn 2017  
Mid-Term Exam Number Two  
November 21, 2017  
Answers

There were two versions, A and B.

Version A: The sphere's radius is 10 meters.

1.  $-1.06 \text{ m}^2/\text{sec}$
2.  $-0.159375 \text{ meters/second}$
3. The absolute maximum is  $0.384901..$  and the absolute minimum is  $0.2629818..$
4. (a)  $l(x) = (\sec^5 4.5 - 1)(x - 4.5) + \tan 4.5 - 4.5 = 21.504848..(x - 4.5) + 0.137332$  (b)  $4.4936139..$
5. There is only one point:  $(\frac{2}{5}, \frac{5}{4})$ .
6. (a)  $x = -\frac{3}{2} + \frac{3}{2} \ln \frac{3}{2}$  (b) Yes,  $y = \frac{1}{2} - \frac{1}{2} \ln \frac{1}{4}$  (c) No:  $t = 0$  and  $t = -1$  are the only places where  $dy/dx$  is undefined, but  $t$  is restricted to  $t > 0$ .

Version B: The sphere's radius is 7 meters.

1.  $-1.3428.. \text{ m}^2/\text{sec}$
2.  $-0.246 \text{ m/sec}$
3. The absolute maximum is  $0.58235..$  and the absolute minimum is  $0.34606..$
4. (a)  $l(x) = (\sec(-2) \tan(-2) - 1)(x + 2) + \sec(-2) + 2$  (b)  $-2.064473$
5. There is only one point:  $(1, \frac{1}{2})$
6. (a)  $x = \frac{2}{5}(-18 + \frac{1}{2} \ln 6) + 6 + \ln 6 = 0.950111..$  (b) No:  $t = 0$  and  $t = -1$  are the only places where  $dy/dx$  is undefined, but  $t$  is restricted to  $t > 0$ . (c) Yes,  $y = \frac{1}{2} - \frac{1}{2} \ln 6$ .