

Math 124 C - Spring 2010  
Mid-Term Exam Number Two  
May 18, 2010

Name: \_\_\_\_\_ Student ID no. : \_\_\_\_\_

Signature: \_\_\_\_\_ Section: \_\_\_\_\_

1	10	
2	10	
3	15	
4	10	
5	10	
6	20	
Total	75	

- Complete all questions.
- You may use a scientific calculator during this examination; graphing calculators and other electronic devices are not allowed and should be turned off for the duration of the exam.
- If you use trial-and-error, a guess-and-check method, or numerical approximation when an exact method is available, you will not receive full credit.
- You may use one double-sided, hand-written, 8.5 by 11 inch page of notes.
- Show all work for full credit.
- You have 80 minutes to complete the exam.

1. Let  $f(x) = \cos(x)$ .

(a) Find the linearization of  $f(x)$  at  $a = \frac{\pi}{4}$ .

(b) Use the linearization to give an approximation of  $\cos(43^\circ)$ .

2. Give the equation of the tangent line to the curve

$$x^3 + y + xy^3 = 65$$

at the point  $(2, 3)$ .

3. For each of the following, determine  $\frac{dy}{dx}$ . Please do not simplify your results.

(a)  $y = x^{\cos x}$

(b)  $y = x \tan^{-1} \left( \frac{1}{x} \right)$

(c)  $x^y = y^x$

4. The volume  $V$  of a cylinder with radius  $r$  and height  $h$  is given by

$$V = \pi r^2 h.$$

A cylinder is growing so that its radius is increasing at the rate of 2 cm per minute and its height is shrinking at the rate of 3 cm per minute.

How fast is the volume of the cylinder changing at the instant that its height is 80 cm and its radius is 50 cm?

5. A man walks away from a street light mounted at the end of a 10 meter high pole. The man walks at the rate of 1 meter/sec. Due to radiation exposure, the man's height is increasing at the rate of 0.01 meter/sec. At the instant the man is 12 meters from the pole, the man is 2 meters tall.

How fast is the length of the man's shadow changing at that instant?

6. An object is moving in the plane with location at time  $t$  seconds given by the parametric equations

$$x(t) = 3 \cos(2t), y(t) = 5 \sin(2t).$$

- (a) The object is moving around an ellipse with equation  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  with  $a > 0$  and  $b > 0$ . Give the values of  $a$  and  $b$ .

- (b) What is the horizontal velocity of the object at time  $t = 1$  ?

- (c) What is the vertical velocity of the object at time  $t = 2$  ?

- (d) Give a time  $t$  when the horizontal and vertical velocities of the object are equal.