

Math 125 H - Winter 2010  
Mid-Term Exam Number One  
January 29, 2010

Name: \_\_\_\_\_

Student ID number: \_\_\_\_\_

Section: \_\_\_\_\_

|       |    |  |
|-------|----|--|
| 1     | 10 |  |
| 2     | 10 |  |
| 3     | 10 |  |
| 4     | 10 |  |
| 5     | 10 |  |
| 6     | 10 |  |
| Total | 60 |  |

- Complete all questions.
- You may use a scientific calculator during this examination; graphing calculators and other electronic devices are not allowed and should be turned off for the duration of the exam.
- If you use trial-and-error, a guess-and-check method, or numerical approximation when an exact method is available, you will not receive full credit.
- You may use one double-sided, hand-written, 8.5 by 11 inch page of notes.
- Show all work for full credit.
- You have 80 minutes to complete the exam.

1. Evaluate the following integrals.

(a)  $\int \frac{dx}{3x^2 + 4}$

(b)  $\int x^9(x^5 + 1)^{12} dx$

2. Evaluate the following integrals.

(a)  $\int_0^\pi (1 + \sin x) (2 + \cos x) \, dx$

(b)  $\int_e^{e^2} \frac{(x+1)(x-1)}{x} \, dx$

3. Give upper and lower bounds for the integral

$$\int_0^1 e^{x^2} dx$$

which differ by less than  $\frac{2}{3}$ .

4. Let  $c > 0$ . The area bounded by  $y = c - x^2$  and the  $x$ -axis equals 3. Find  $c$ .

5. Consider the region bounded by  $y = x^2 - x$  and the  $x$ -axis. Find the volume of the solid of revolution created by revolving this region about the  $y$ -axis.

6. Consider the region bounded by  $y = 5 - \frac{1}{4}x^2$  and  $y = x^2$ . Find the volume of the solid of revolution created by revolving this region about the  $x$ -axis.