Math 125A - Spring 2003 Mid-Term Exam Number Two April 24, 2003

Name: _____

Section:

1	10	
2	10	
3	10	
4	10	
5	10	
6	10	
7	10	
Total	70	

- This exam consists of 7 problems. Be sure that you complete all 7 problems.
- You may use a scientific (non-graphing) calculator during this examination. Other electronic devices are not allowed.
- You may use one hand-written 8.5 by 11 inch page of notes. You can use both sides of the note page.
- Show all work for full credit.
- Unless the problem specifies an approximation, an exact answer should be given.
- Mechanisms are in place to render cheating detectable and ineffective.
- You have 80 minutes to complete the exam.

1. Consider the region in the first quadrant bounded by $y = x^{\frac{3}{2}}$, x = 0 and y = 8. Suppose this region is revolved about the y-axis to create a three-dimensional solid. Suppose we have a tank with the shape of that solid, oriented so that the y-axis is perpendicular to the ground, the origin is at the bottom of the tank, and units are in meters (so the tank is 8 meters tall). If the tank is filled with a liquid with density 2300 kg/m³, how much work is required to pump all of the liquid to the top of the tank?

2. For what k > 0 do $y = x^2$ and $y = 10 - x^2$ have the same average value on the interval [0, k]?

3. Use Simpson's Rule with n = 6 to approximate the integral:

$$\int_{2}^{5} \frac{1}{\ln x} \, dx$$

Maintain at least 4 digits of precision at all times.

4. Evaluate each of the following integrals:

(a)
$$\int x^5 \ln x \, dx$$

(b) $\int \sin^3 x \cos^6 x \, dx$

5. Evaluate each of the following integrals:

(a)
$$\int \frac{3 \, dx}{x^2 + 3x - 10}$$

(b)
$$\int \frac{5 \, dx}{x^2 + 8x + 20}$$

6. Evaluate the following integrals.

(a)
$$\int \frac{dx}{\sqrt{x^2 - 8x + 18}}$$

(b)
$$\int \frac{dx}{x^3 + 3x^2}$$

7. Evaluate the following integrals.

(a)
$$\int x^3 e^{x^2} dx$$

(b)
$$\int \frac{dx}{(x^2-1)^{\frac{5}{2}}}$$