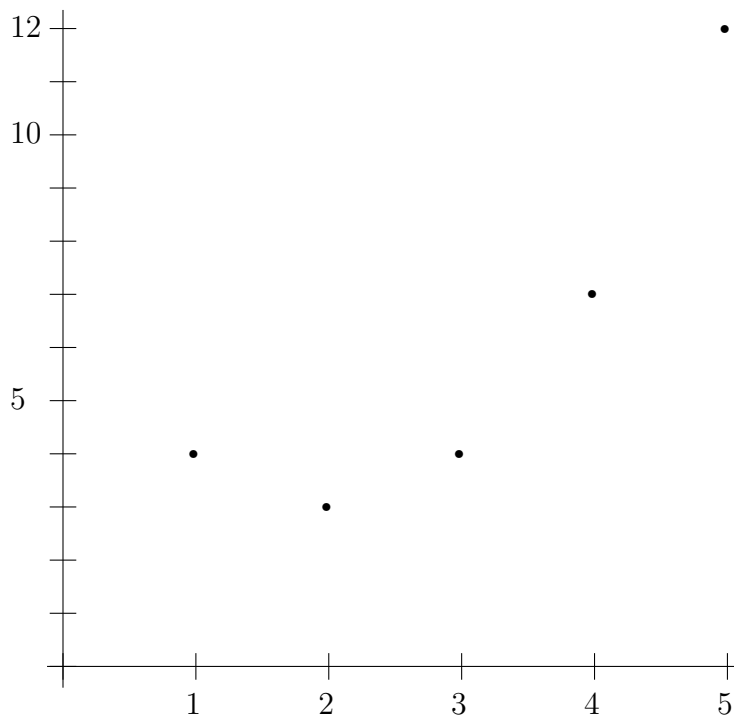


**M145 Worksheet # 3** Thurs, Jan 19, 2006

**(1a)** Below is the graph of a function  $y = f(x)$ , with the values of  $f(x)$  marked at the points  $x = 1, 2, 3, 4, 5$ . Give lower (L) and upper (U) bounds for the area under the curve from  $x = 1$  to  $x = 5$ .

For (L) use 4 rectangles, with  $\Delta x = 1$  and min value of  $f(x)$  to calculate the height.

For (U) use 4 rectangles also with  $\Delta x = 1$  and max value of  $f(x)$  to calculate the height.



**(1b)** Use the trapezoid rule (with  $\Delta x = 1$ ) to find a good estimate for the area.

**(1c)** You are told that the function in **(1a)** is  $y = x^2 - 4x + 7$ . Use the Fundamental Theorem to calculate (exactly) the area under the curve from  $x = 1$  to  $x = 5$ .