

### Proof writing tips

- The intended audience for your proofs are your classmates. Write a proof in such a way that your classmates can easily understand what you are doing.
- Explain what you are doing in plain English. Use complete sentences, following the same conventions of grammar, punctuation, spelling as any other writing.
- Clearly explain the meaning of any new quantity or symbol you introduce.
- Label your formulas.
- Pay attention to quantifiers. If you write  $f(a) > 0$ , do you mean to say that this is true **for all**  $a \in R$ , that **there exists some**  $a \in R$  for which this is true, or that that this is true for a **particular**  $a$  you have in mind or you introduced before?
- Pay attention to the difference between a statement and a formula. " $\sum_{i=1}^5 i = 15$ " is a statement, while " $\sum_{i=1}^5 i$ " is a formula and it does not make sense to say something like "assume  $\sum_{i=1}^5 i$ " or "I need to prove  $\sum_{i=1}^5 i$ " or " $\sum_{i=1}^5 i$  implies the following" ...."
- When you write something like " $x = 2$ " that means you are stating that under the hypothesis of the theorem you are proving  $x$  must be equal to 2 and no other value. If you write "**assume**  $x = 2$ " it means that you are considering what happens when  $x = 2$ , but the hypothesis of your theorem do not imply  $x$  must be equal to 2 (and in your proof you may also have to consider the case when  $x$  is different from 2). Clearly state your assumptions (that is do not write  $x = 2$ , when you really mean "**assume**  $x = 2$ ").
- Identify any theorems you are using from the book, previous homework, lectures....
- Make sure you reread your proofs (ideally a while after you have written them).