

**Chapter 3 [Pugh, pg. 198]:** 19, 27(b), 28(i $\Leftrightarrow$ ii).

**Additional problems**

1. Prove that the rational ruler function is continuous at each irrational  $x \in [0, 1]$ .
2. Let  $S \subset \mathbb{R}$ . Show that  $\text{osc}_x(\chi_S) = 1$  if  $x \in \partial S$  and  $\text{osc}_x(\chi_S) = 0$  if  $x \notin \partial S$ .