Math 427

## Homework 1

Autumn 2019
Due Friday, October 4

Section 1.1: 5, 11, 15
Section 1.2: 1, 2
Section 1.3: 4, 6, 9

## Additional problems

1. Consider $z=1+3 i$ and $w=2-5 i$. Plot $z, w, z+w$ in the plane, find $|z|,|w|,|z+w|$, and check that the triangle inequality holds (you can use your calculator to check).
2. Use the ratio test to find the radius of convergence for the following series:

$$
\begin{aligned}
& \frac{1}{2} z-\frac{1}{4} z^{2}+\frac{1}{6} z^{3}-\frac{1}{8} z^{4}+\cdots=\sum_{j=1}^{\infty} \frac{(-1)^{j+1}}{2 j} z^{j} \\
& \frac{z}{2}+\frac{z^{3}}{4}+\frac{z^{5}}{8}+\frac{z^{7}}{16}+\cdots=\sum_{j=0}^{\infty} \frac{z^{2 j+1}}{2^{j+1}}
\end{aligned}
$$

