

NAME \_\_\_\_\_

QUIZ SECTION \_\_\_\_\_

MIDTERM II  
Math 126, Section A  
February 22, 2007

Problem	Total Points	Score
1	12	
2	12	
3	12	
4	14	
Total	50	
5(Bonus)	3	

- You may use a scientific calculator and one one-sided sheet of handwritten notes. No other notes, books or calculators are allowed. Please turn off your cell phone.
- Show all your work to get full credit.
- Read instructions for each problem CAREFULLY.
- Leave all your answers in EXACT form.
- Check your work!

1. (12pts) Consider the curve given by the equation in polar coordinates

$$r = 4 \cos \theta + \sin \theta.$$

(a)(6pts) Find the Cartesian equation of the curve. Sketch the curve.

(b)(6pts) Find the equation of the tangent line to the curve at the point  $\theta = \pi/4$ .

2. (12pts) Consider the parametric curve given by the vector function  $\vec{r}(t) = (t, t^2, t^3)$ .  
(a)(4pts) Find the equation of the normal plane to the curve at the point when  $t = 1$ .

*Hint.* The normal plane is the plane perpendicular to the tangent line.

- (b)(4pts) Find the equation of the normal plane to the curve at the point  $(-1, 1, -1)$ .

- (c)(4pts) Find the parametric equations of the line of intersection of the planes from (a) and (b).

3. (12pts) Consider the surface defined by the equation  $f(x, y) = x^2y + y^3 + x$ .
- (a)(6pts) Find the tangent plane to the surface at the point  $(-2, 1, 3)$ .

(b)(6pts) Find all second partial derivatives of  $f(x, y)$ .

4. (14pts) (a)(5pts) Find the velocity and position vectors of a particle that has the acceleration vector

$$\vec{a}(t) = (2, \cos t, \sin t),$$

the initial velocity  $\vec{v}(0) = \langle 0, 0, -1 \rangle$  and the initial position  $\vec{r}(0) = \langle 1, 1, 0 \rangle$ .

- (b)(1pt) Find the position vector at the time  $t = 1$ .

Answer the following two questions in any order. Simplify your answers as much as possible.

(c)(4pts) Find the curvature at  $t = 1$ .

(d)(4pts) Find the length of the projection of the acceleration vector at  $t = 1$  on the unit normal vector at  $t = 1$ .

5. (3pts) (*Bonus, full credit only*). Show that if a particle moves with the constant speed, then the velocity and acceleration vectors are orthogonal.