Sample MIDTERM 2 Last year's midterm for Spring MATH 126 A, B

Scientific, but not graphing calculators are OK.

You may use one 8.5 by 11 sheet of handwritten notes.

Problem 1. Consider a particle traveling according to the equations

 $x(t) = \cos^2 t, \quad y(t) = \cos t.$

Write down and simplify (but do not evaluate) the formula for the length of the curve along which the particle is moving.

Problem 2. Consider a particle whose velocity, at time $t \ge 0$, is given by

$$\vec{v}(t) = \langle -2t, -\sin t \rangle$$

and whose position at t = 0 is (4, 0).

a. Find the formula for the position of the particle at time t.

b. Find the point at which the particle crosses the y axis.

c. Suppose the acceleration suddenly drops to 0 at the time when the particle crosses the y-axis, so that there are no forces acting on the particle. Find the position of the particle one minute later.

Problem 3. Find the equations of the <u>normal</u> and of the <u>osculating</u> planes to the curve

$$\vec{r}(t) = \langle t^3, \sin(\pi t), t+1 \rangle$$

at the point corresponding to t = 2.

Problem 4. Identify the curve

$r = 2\sin\theta + 2\cos\theta$

by finding a Cartesian equation for the curve. Give a verbal description of what that curve is.

Problem 5. Consider the function of two variables

$$f(x,y) = \sqrt{1 + x - y^2}.$$

a. Identify and sketch the domain of f(x, y).

b. Find the partial derivatives $f_y(x, y)$ and $f_x(x, y)$.

c. Find the second partial derivative $f_{xy}(x, y)$.

d. Find an equation of the tangent plane at the point (1, 1).