

Assignment #5: Due Friday, 2/17/12

Reading:

- Sections 2.1, 2.2, 2.3, and 2.4.

Written Assignment:

- Exercise 2.19 (p. 38).
- Exercise 2.24 (p. 39).
- Exercise 2.25 (p. 39).
- Let $H \subset \mathbb{R}^2$ be the right half-plane, defined by

$$H = \{(u, v) : u > 0\}.$$

Suppose $C \subset H$ is a simple curve (see Example 2.18). The *surface of revolution determined by C* is the set $S_C \subset \mathbb{R}^3$ defined by

$$S_C = \{(x, y, z) : (s(x, y), z) \in C\},$$

where $s(x, y) = \sqrt{x^2 + y^2}$. The simple curve C is called the *generating curve* for the surface. Show that S_C is a regular surface.

- Let $f: \mathbb{R}^3 \rightarrow \mathbb{R}$ be the function $f(x, y, z) = x^2 - 2xy + y^2$. Which level sets of f are regular surfaces? For each level set, either prove it is a regular surface or prove it is not.