

---

Instructions: You have 30 minutes. You **MUST** show work for credit. If in doubt, ask for clarification.

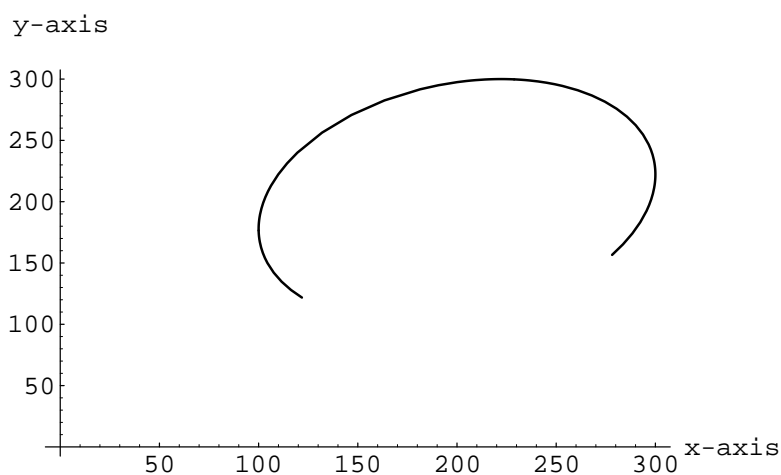
---

1. (5 points) A point is moving in the  $xy$ -coordinate system according to the parametric equations:

$$x(t) = 100 \sin\left(\frac{2\pi}{7}(t - 6)\right) + 200$$

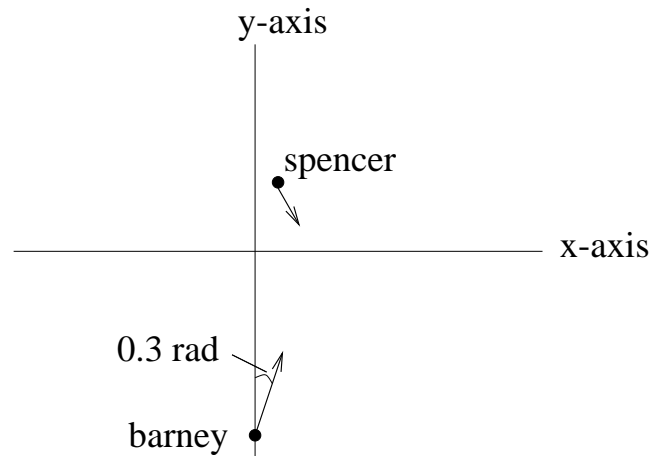
$$y(t) = 100 \sin\left(\frac{2\pi}{7}(t - 0.5)\right) + 200$$

where  $t$  represents time in seconds and  $0 \leq t \leq 5$ . Here is a graph of this parametrized curve.



- (a) (3pts) Where is the object located at time  $t = 0$  seconds? (Find the coordinates and mark in the picture.)  
 $P(0) = (278.2, 156.6)$ ; point should be labeled on the curve.
- (b) (1pts) Which direction is the point moving along the curve? (Indicate with some sort of arrow.)  
Moves from  $P(0)$  in part (a) to the other end of the curve.
- (c) (1 pts) Can you find a function  $y = f(x)$  whose graph is this parametrized curve? (Justify)  
No; curve violates the vertical line test.

2. Barney and Spencer start at the two locations pictured in the  $xy$ -coordinate system; the units on each axis will be meters. Barney is initially located at the point  $(0,-8)$  and has a speed of 3 meters/sec in the direction indicated. Spencer has parametric equations:  $S(t) = (x_S(t), y_S(t))$ , where  $x_S(t) = 1 + t$ ,  $y_S(t) = 3 - 2t$ . Barney and Spencer start moving at the same time.



- (a) (2pts) Find Spencer's initial coordinates at time  $t = 0$ .  
 $(1, 3)$
- (b) (1pts) Find the time when Spencer crosses the  $x$ -axis.  
 Solve  $y_S(t) = 0$ ; get  $t = 3/2$ , plug into  $S(3/2) = (5/2, 0)$  to be the place Spencer crosses the  $x$ -axis.
- (c) (5pts) Find parametric equations for Barney's motion.  
 Resolve Barney's velocity vector; the direction angle is  $\frac{\pi}{2} - 0.3 = 1.271$  rad. Get  $v_x = 0.886$  m/s and  $v_y = 2.866$  m/s. Conclude Barney's position at time  $t$  is given by  $B(t) = (0.886t, -8 + 2.866t)$ .
- (d) (4pts) Find the distance between Barney and Spencer at time  $t$ . Your answer should be a function in the variable  $t$ . Use your formula to calculate the distance between these guys at time  $t = 2$  seconds.  
 Use the distance formula to get  $d(t) = \sqrt{(.886t - 1 - t)^2 + (-8 + 2.866t - 3 + 2t)^2}$  This answer is ok, could simplify to get  $d(t) = \sqrt{23.691t^2 - 106.82t + 122}$ . Calculate  $d(2) = 1.77$  meters.
- (e) (3pts) What is the velocity vector for Spencer? (You need to specify Spencer's speed and direction.)  
 Speed is  $|v| = \sqrt{(-2)^2 + 1} = 2.24$  m/s. Direction is  $\theta = -1.107$  rad or  $\theta = 5.176$  rad.