MATH 126 - Winter 2009
Final Exam Answers

1. (a) $x+y=2$
(b) $\left(\frac{3}{2}, \frac{1}{2},-5\right)$
2. $(2,2)$ and $(-2,2)$
3. The minimum speed is 3 feet per second.
4. (a) $T_{2}(x)=1+2(x-1)+\frac{3}{2}(x-1)^{2}$
(b) $F(0.8) \approx 0.66$
(c) One acceptable answer is $\left|F(x)-T_{2}(x)\right| \leq \frac{4}{6}|0.2|^{3}$. (A larger bound might be acceptable with the appropriate work.)
5. (a) The Taylor series for $f(x)$ based at $b=0$ is:

$$
1+\sum_{k=0}^{\infty} \frac{(-1)^{k} 3^{k+1}}{e^{k+1}(k+1)} x^{k+1}
$$

(b) The series converges for $|x|<\frac{e}{3}$.
6. (a) $x=-t, y=1, z=\pi+2 t$
(b) $y=1$
7. (a) The domain is all points on and inside the circle centered at $(e, e)$ with radius $5 e$ that lie above the line $y=x$.
(b) $-\frac{4}{3}(x-e)+\left(\frac{4}{3}-\frac{3 \ln 3 e}{4}\right)(y-4 e)-(z-4 e \ln 3 e)=0$
8. (a) Here's what $D$ looks like:

(b) $\frac{2 \pi}{3}+\sqrt{3}$
9. There is a saddle point at $(0,0)$ and a local minimum at $\left(\frac{9}{2}, 3\right)$.

