MATH 126 – Winter 2009 Final Exam Answers

1. (a) x + y = 2(b) $\left(\frac{3}{2}, \frac{1}{2}, -5\right)$

2. (2,2) and (-2,2)

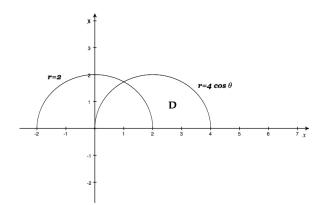
- 3. The minimum speed is 3 feet per second.
- 4. (a) $T_2(x) = 1 + 2(x-1) + \frac{3}{2}(x-1)^2$
 - (b) $F(0.8) \approx 0.66$
 - (c) One acceptable answer is $|F(x) T_2(x)| \le \frac{4}{6}|0.2|^3$. (A larger bound might be acceptable with the appropriate work.)
- 5. (a) The Taylor series for f(x) based at b = 0 is:

$$1 + \sum_{k=0}^{\infty} \frac{(-1)^k 3^{k+1}}{e^{k+1}(k+1)} x^{k+1}.$$

- (b) The series converges for $|x| < \frac{e}{3}$.
- 6. (a) x = -t, y = 1, $z = \pi + 2t$ (b) y = 1
- 7. (a) The domain is all points on and inside the circle centered at (e, e) with radius 5e that lie *above* the line y = x.

(b)
$$-\frac{4}{3}(x-e) + \left(\frac{4}{3} - \frac{3\ln 3e}{4}\right)(y-4e) - (z-4e\ln 3e) = 0$$

8. (a) Here's what D looks like:



(b) $\frac{2\pi}{3} + \sqrt{3}$

9. There is a saddle point at (0,0) and a local minimum at $\left(\frac{9}{2},3\right)$.