MATH 126 FINAL EXAM ANSWERS WINTER 2013

1. (a) No. One possible justification is: the plane through (2,2,2), (1,0,0), and (2,3,7) is 8x - 5y + z = 8 and $8(5) - 5(5) + 5 \neq 8$.

(b)
$$\frac{13}{90} \langle 8, -5, 1 \rangle = \left\langle \frac{52}{45}, \frac{-13}{18}, \frac{13}{90} \right\rangle$$

2. (a)
$$\mathbf{T}(t) = \left\langle \frac{2}{t+2}, \frac{t}{t+2}, \frac{2t^{1/2}}{t+2} \right\rangle$$

(b)
$$2(x-2) + (y-\frac{1}{2}) + 2(z-\frac{4}{3}) = 0$$

(c)
$$\kappa(t) = \frac{1}{\sqrt{t(t+2)^2}}$$
 and $\lim_{t\to\infty} \kappa(t) = 0$. The curve gets "straighter" as $t\to\infty$.

- 3. (a) i. point; ii. ellipse; iii. pair of lines; iv. hyperbola; v. pair of lines; vi. hyperbola.
 - (b) cone
 - (c) T, T

4.
$$x + y + z = 3$$

5. (a)
$$z = -3(x-2) + 8(y-2) - 6$$

(b)
$$-6.43$$

6. 18 inches by 18 inches by 36 inches

7. (a)
$$\frac{1}{3}\sin 1$$

(b)
$$2\pi \left[\frac{1000 - 2(50)^{3/2}}{3} \right]$$

8. (a)
$$x^3 e^{x^2} = \sum_{k=0}^{\infty} \frac{x^{2k+3}}{k!}$$
 for all real x

(b)
$$T_5(x) = x^3 + x^5$$

(c)
$$g(x) = \sum_{k=0}^{\infty} \frac{x^{2k+4}}{(2k+4)k!}$$
 for all real x

9. (a)
$$T_2(x) = 2 + \frac{1}{12}(x-8) - \frac{1}{288}(x-8)^2$$

(b)
$$|f(x) - T_2(x)| \le \frac{10}{6 \cdot 27 \cdot 7^{8/3}} \approx 0.0003443$$
 (Larger bounds accepted.)

(c)
$$\sqrt[3]{9} \approx \frac{599}{288} \approx 2.07986$$