

MATH 126 – EXAM II Hints and Answers  
Version Alpha  
Autumn 2009

1. (a) (7 points) HINT:  $r'(2) = \langle 4, -2, 6 \rangle$  and  $r''(2) = \langle 2, 1, 1 \rangle$ .  
ANSWER:  $a_T = \frac{12}{\sqrt{56}}$  and  $a_N = \frac{8\sqrt{3}}{\sqrt{56}}$
- (b) (3 points) ANSWER:  $4(x - 4) - 2(y + 5) + 6(z - 10) = 0$  OR  $4x - 2y + 6z = 86$  OR  $2x - y + 3z = 43$
2. (a) (4 points) HINT:  $f_y(x, y) = -e^{-xy}(\sin y + x \cos y)$   
ANSWER:  $f_{yx}(x, y) = -e^{-xy}(\cos y - y \sin y - xy \cos y)$
- (b) (4 points) HINT:  $f_x(x, y) = -ye^{-xy} \cos y$ . So,  $f_x(\pi, 0) = 0$  and  $f_y(\pi, 0) = -\pi$ . The tangent plane is the plane with normal vector  $\langle 0, -\pi, -1 \rangle$  that contains the point  $(\pi, 0, f(\pi, 0)) = (\pi, 0, 1)$ .  
ANSWER:  $-\pi(y - 0) - 1(z - 1) = 0$  OR  $z = 1 - \pi y$
- (c) (2 points) ANSWER:  $f(3.15, 0.001) \approx 1 - 0.001\pi \approx 0.9968584$
3. (a) (8 points) HINT:  $g_x(x, y) = x + y - 3$  and  $g_y(x, y) = x + y^2 - 3$ .  
ANSWER: There is a saddle point at  $(3, 0)$  and a local minimum at  $(2, 1)$ .
- (b) (2 points) HINT:  $g(x, 0) = \frac{1}{2}x^2 - 3x$ , a quadratic whose graph is a parabola that opens up. Its vertex occurs at  $x = 3$ .  
ANSWER:  $g(3, 0) = -\frac{9}{2}$
4. HINT: You must change the order of integration! With the current order, you have  $0 \leq x \leq \sqrt{\pi/2}$  and  $x \leq y \leq \sqrt{\pi/2}$ . This means, the region over which you are integrating is the triangle bounded on the left by the  $y$ -axis ( $x = 0$ ), below by the line  $y = x$  and above by the line  $y = \sqrt{\pi/2}$ .

Then, we have:

$$\int_0^{\sqrt{\pi/2}} \int_x^{\sqrt{\pi/2}} \cos(y^2) dy dx = \int_0^{\sqrt{\pi/2}} \int_0^y \cos(y^2) dx dy.$$

ANSWER:  $\frac{1}{2}$

5. HINT: Convert to polar:

$$\iint_D \frac{xye^x}{(x^2 + y^2)^{3/2}} dA = \int_0^{\pi/2} \int_0^3 \cos \theta \sin \theta e^{r \cos \theta} dr d\theta.$$

ANSWER:  $\frac{1}{3}e^3 - \frac{4}{3}$