## UW Math Circle - Homework 4



1. In class we showed how to construct equilateral triangles and $90^{\circ}$ angles using only a compass and straight edge. Show how to construct a square using a compass and a straight edge. Now, show how to construct a regular hexagon (a regular hexagon is just a hexagon with all sides equal in length).
2. Given a circle with center O and radius R , construct a second circle that is tangent to the first (tangent means that the two circles touch in exactly one point).

3. Given points $\mathrm{X}, \mathrm{Y}$, and O that do not lie on a line:
a) Construct any line parallel to XY.
b) Construct a line parallel to XY that goes through O.
4. Challenge: Suppose you know how to bisect an angle. This means that given some angle ABC , you know how to construct the angle bisector of ABC. Using this, show how you can construct any regular $2^{n}$-gon (a regular $2^{n}$ gon is a polygon with $2^{n}$ sides which has all sides equal in length). A regular 16 -gon $(n=4)$ is shown below.

