# UW Math Circle 

April 3, 2014

1. Find the area of the polygon below.

2. Let's say that a lattice point on a piece of graph paper is a point where two grid lines meet.
(a) Count the number of lattice points inside the polygon above (not touching the boundary).
(b) Count the number of lattice points on the boundary of the polygon.
3. Draw more polygons on your graph paper. For each one, find its area $(A)$ and count the number of lattice points inside the polygon, $(I)$, and the number of the lattice points on the boundary $(B)$. Experiment with different polygons and write down your results!
4. Come up with a formula relating $A$ to $I$ and $B$.
5. Prove your formula is correct!
