# UW Math Circle 

February 19, 2015

1. Trominoes, revisited! A tromino is an L-shaped piece, drawn below. Is it possible to cover an $2^{n} \times 2^{n}$ chessboard with any square removed with trominoes?

2. Prove that the sum of degrees of the interior angles of an $n$-gon is $(n-2) 180$.

3. Prove that $7^{n}-1$ is a multiple of 6 for all positive integers $n$.
4. Prove that the number $111 \ldots 111\left(3^{n} 1\right.$ 's) is divisible by $3^{n}$.
5. Find a formula for the number of ways to cover a $2 \times n$ chessboard with dominoes (so that each square is covered, and no dominoes overlap). Prove your formula is correct.
