

## Announcements

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- This week: Final Exam Review
- Homework #10A & 10B Due Wednesday, December 7. 11:00pm
- Bring ReviewOne.pdf and ReviewTwo.pdf to your TA sections this week
- Course evaluations are now open. Your input really matters!
  - ▶ 125A: <https://uw.iasystem.org/survey/165334> (68% completed)
  - ▶ 125B: <https://uw.iasystem.org/survey/165324> (85% completed!)
- Final Exam: Saturday, December 10 from 1:30 – 4:20 pm (Bring UW ID)
  - ▶ Go to the correct Room: 125 A in KNE 110 and 125 B in KNE 210
  - ▶ Cumulative Exam: Covers all material
  - ▶ The only calculator allowed is the Ti-30x IIS.
  - ▶ Allowed one 8.5 x 11 sheet of notes (both sides)
  - ▶ May use the 20 integrals on p. 495 without deriving them. Show your work in evaluating any other integrals, even if on your note sheet.
  - ▶ CLUE final exam review Friday: 7-9 pm in MGH 389.

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### Today

- Final Exam Review - Requested problems

**Autumn 2013, Problem 7.** The stale air in a crowded exam room initially contains  $6.25 \text{ ft}^3$  of carbon dioxide ( $\text{CO}_2$ ). An air conditioner is turned on at time  $t = 0$  and blows fresher air into the room at a rate of  $500 \text{ ft}^3/\text{min}$ . The fresher air mixes with the stale air (assume it mixes instantaneously) and the well-mixed air leaves the room at the same rate of  $500 \text{ ft}^3/\text{min}$ . The incoming fresher air contains  $0.01\%$   $\text{CO}_2$  (by volume), and the air in the room has a total volume of  $2500 \text{ ft}^3$ . By their breathing, the people in the room generate an additional  $0.08 \text{ ft}^3$  of  $\text{CO}_2$  per minute (without changing the total volume of air in the room). Let  $y(t)$  denote the amount (in  $\text{ft}^3$ ) of  $\text{CO}_2$  in the room,  $t$  minutes after the air conditioner is turned on.

- 1 Find a differential equation satisfied by  $y(t)$ . Simplify the differential equation, but wait until part (b) to solve it.
- 2 Now solve the differential equation from part (a), and solve for any constant(s) in your solution to find a formula for  $y(t)$ .

**Autumn 2013, Problem 5.** Find the coordinates of the center of mass of a circular plate of radius 1 with center at the origin  $(0, 0)$  made with a material whose density is 2 on the upper semicircular region and 1 on the lower semicircular region.

**Winter 2005, Problem 5.** Let  $b$  be a positive number, and consider the region bounded by the curves

$$y = x^2, \quad y = x^2 + 1, \quad x = -b, \quad \text{and} \quad x = b.$$

- 1 Find the  $y$ -coordinate of the center of mass of this region, in terms of  $b$ .
- 2 Because of the symmetry of this region, the  $x$ -coordinate of the center of mass is 0. For small values of  $b$ , say  $b < M$ , the center of mass is in the region, while for  $b > M$ , the center of mass is outside of the region. Find  $M$ .