

MATH 112 - Winter 2005
Exam 1, Version 2 - Hints and Answers

1. (a) (2 points) HINT: $g(x)$ decreases when $g'(x)$ is below the x -axis
ANSWER: from 0 to 3 and from 6 to 10
 - (b) (2 points) HINT: $f'(x)$ is above the x -axis when $f(x)$ is increasing
ANSWER: from 0 to 2 and from 5 to 8
 - (c) (3 points) HINT: $g(x)$ has a horizontal tangent line when $g'(x)$ crosses the x -axis
ANSWER: $x = 3, 6,$ and 10
 - (d) (3 points) HINT: $f'(x)$ crosses the x -axis when $f(x)$ has a horizontal tangent line.
ANSWER: $x = 2, 5,$ and 8
 - (e) (1 point) ANSWER: iii
2. (4 points each)
 - (a) HINT: $y = x^{2/3} + 7x^{-1/3}$
ANSWER: $\frac{dy}{dx} = \frac{2}{3}x^{-1/3} + 7\left(-\frac{1}{3}x^{-4/3}\right)$
 - (b) HINT: $R(q) = q^8 - 4q^5$
ANSWER: $R'(q) = 8q^7 - 20q^4$
 - (c) HINT: $s = 4t^8 - t + 3$
ANSWER: $\frac{ds}{dt} = 32t^7 - 1$
3. (a) (3 points) HINT: You're looking for $\frac{A(6 + 0.5) - A(6)}{0.5}$. So, take $t = 6$ and $m = 0.5$ in the given formula.
ANSWER: 7.5 thousand gallons per hour
 - (b) (4 points) HINT: Take $t = 4$ and $m = h$ and use the given formula to compute $\frac{A(4 + h) - A(4)}{h}$. Multiply both sides by h to get $A(4 + h) - A(4) = 12h - h^2$. Set this equal to 36 and solve for q .
ANSWER: $h = 6$
 - (c) (4 points) HINT: You want to compute $A'(5.46)$. You have a formula for the slope of the secant line through $A(t)$ at t and $t + m$. To get $A'(t)$, let m go to zero: $A'(t) = 20 - 2t$.
ANSWER: $A'(5.46) = 9.08$ thousand gallons per hour

- (d) (4 points) HINT: You know that $A(4) = 9$ and you want $A(7)$. Take $t = 4$ and $m = 3$ and use the given formula to compute $\frac{A(7) - A(4)}{3}$. Multiply by 3 to get $A(7) - A(4) = 27$. Now use the fact that $A(4) = 9$ and solve for $A(7)$.

ANSWER: $A(7) = 36$ thousand gallons

4. (4 points each)

- (a) HINT: Speed is the derivative of distance. So, Bert's speed is $B'(t) = -2t + 16$ and Ernie's is $E'(t) = 2t$. You need to solve the equation $E'(t) = B'(t) + 7.72$ for t .

ANSWER: $t = 5.93$ minutes

- (b) HINT: $B(1 + h) = -(1 + h)^2 + 16(1 + h) = -h^2 + 14h + 15$ and $B(1) = 15$.

ANSWER: $B(1 + h) - B(1) = (-1)h^2 + (14)h + (0)$

- (c) HINT: Solve $B'(t) = 6.24$ for t : $t = 4.88$. Compute $E(4.88)$.

ANSWER: 23.8144 feet (rounding to 21.81 feet is OK)