

Exam I Hints and Answers
Math 126 D Spring 2011

1. (a) ANSWER: $(-2, 14, 6)$
(b) ANSWER: $y - 2z = 2$

2. HINT: $x = r \cos \theta = (6 + \cos(6\theta)) \cos \theta$, $y = r \sin \theta = (6 + \cos(6\theta)) \sin \theta$, and $\frac{dy}{dx} = \frac{dy/d\theta}{dx/d\theta}$.

ANSWER: $y = -\sqrt{3}x + 10$

3. (a) HINT: $\overrightarrow{PQ} = \langle k - 3, -3, 0 \rangle$, $\overrightarrow{PS} = \langle -5, -4, 2 \rangle$, and $|\overrightarrow{PQ} \times \overrightarrow{PS}| = \sqrt{581}$.
ANSWER: $k = 5$

- (b) HINT: Let R be the point with coordinates (x, y, z) . Then $\overrightarrow{QR} = \langle x - 5, y - 1, z - 1 \rangle$ and $\overrightarrow{QR} = \overrightarrow{PS}$.

ANSWER: $(0, -3, 3)$

4. (a) ANSWER: $\vec{T}(t) = \langle -\frac{3}{5} \sin 3t, \frac{4}{5}, \frac{3}{5} \cos 3t \rangle$ and $\vec{N}(t) = \langle -\cos 3t, 0, -\sin 3t \rangle$

- (b) HINT: The direction vector for the line of intersection of two planes is any vector that is orthogonal to both planes.

A vector that is orthogonal to the normal plane is $\vec{n}_1 = \vec{T} \left(\frac{\pi}{12} \right)$. A vector that is orthogonal to the osculating plane is $\vec{n}_2 = \vec{B} \left(\frac{\pi}{12} \right)$. Note that the unit normal vector is parallel to the cross-product of $\vec{n}_1 \times \vec{n}_2$. So, the unit normal vector may be used as the direction vector of the line of intersection: $\vec{v} = \vec{N} \left(\frac{\pi}{12} \right)$.

ANSWER: $x = \frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}t$, $y = \frac{\pi}{3}$, $z = \frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}t$