February 22, 2008

## Office hours today 1:30-2:30 Math lounge Padelford C-wing 1st floor

## Problem 1

Given $(a, b, c, d) \in \mathbb{R}^{4}$, let $f: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ be defined by

$$
f(x, y)=(a x+b y, c x+d y) .
$$

Prove that $f$ injective if and only if $a d-b c \neq 0$.

## Problem 2

Given $(a, b, c, d) \in \mathbb{R}^{4}$, let $f: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ be defined by

$$
f(x, y)=(a x+b y, c x+d y) .
$$

Prove that $f$ surjective if and only if $a d-b c \neq 0$.

