## Math 525

## Homework due 02/11/2015

Reading from Folland: Chapter 5: sections 1, 2 and 3.

Problems from Folland: Chapter 5: problems 7, 11, 12 and 15.

Problem 1: Let

$$\mathcal{H} = \left\{ u : \mathbb{R}^n \to \mathbb{R} : u \text{ continuous and } \forall x \in \mathbb{R}^n, \forall r > 0, \ u(x) = \frac{1}{m(B(x,r))} \int_{B(x,r)} u(y) \, dy \right\}$$

Show that if  $\{u_n\}_{n=1}^{\infty} \subset \mathcal{H}$  is uniformly bounded on compact subsets of  $\mathbb{R}^n$ , there exists a subsequence that converges uniformly to a function  $u \in \mathcal{H}$  on compact subsets of  $\mathbb{R}^n$ .