

# Zihui ZHAO

## PERSONAL DATA

---

ADDRESS: Department of Mathematics, 404 Krieger Hall  
3400 N. Charles Street, Baltimore, MD 21218  
OFFICE: Krieger 303  
EMAIL: [zhaozh@jhu.edu](mailto:zhaozh@jhu.edu)  
WEBSITE: <https://zhaozh.xyz>

## EMPLOYMENT

---

2023 - | Tenure-track Assistant Professor, **Johns Hopkins University**  
2019 - 2023 | NSF Postdoc and L.E. Dickson Instructor, **University of Chicago**  
2018 - 2019 | Member, **Institute for Advanced Study**  
special year program on *Variational methods in geometry*

## EDUCATION

---

2013 - 2018 | Ph.D. in Mathematics, **University of Washington**  
Thesis: Analytic and geometric aspects of the elliptic measure on non-smooth domains  
Advisor: Prof. Tatiana TORO  
Spring 2017 | Program associate at the Harmonic Analysis program, **MSRI Berkeley**  
2011 - 2013 | M.S. in Mathematics, **École Normale Supérieure/Université Paris-Sud XI**  
Thesis: Minimal mass blow-up for the critical generalized Korteweg-de Vries Equation  
Advisor: Prof. Yvan MARTEL  
2007 - 2011 | B.S. in Mathematics, **Peking University**

## PUBLICATIONS & PREPRINTS

---

1. *A note on the critical set of harmonic functions near the boundary.* (with Carlos Kenig), arXiv:2402.08881
2. *Elliptic operators in rough sets, and the Dirichlet problem with boundary data in Hölder spaces.* (with Mingming Cao, Pablo Hidalgo-Palencia, José María Martell, Cruz Prisuelos-Arribas), arXiv:2311.03270
3. *Examples of non-Dini domains with large singular sets.* (with Carlos Kenig) *Advanced Non-linear Studies Special Issue: In honor of David Jerison*, **23** (2023), no. 1.
4. *Expansion of harmonic functions near the boundary of Dini domains.* (with Carlos Kenig) *Rev. Mat. Iberoam.* **38** (2022), no. 7, 2117-2152.

5. *Elliptic measures for Dahlberg-Kenig-Pipher operators: Asymptotically optimal estimates.* (with Simon Bortz, Tatiana Toro) *Math. Ann.*, **385** (2023), 881-919.
6. *Boundary unique continuation on  $C^1$ -Dini domains and the size of the singular set.* (with Carlos Kenig) *Arch. Ration. Mech. An.*, **245** (2022), 373-374.
7. *Optimal Poisson kernel regularity for elliptic operators with Hölder-continuous coefficients in vanishing chord-arc domains.* (with Simon Bortz, Tatiana Toro) *J. Funct. Anal.*, **285** (2023), no. 5.
8. *Uniform rectifiability and elliptic operators satisfying a Carleson measure condition. Part II: the large constant case.* (with Steve Hofmann, José María Martell, Svitlana Mayboroda, Tatiana Toro) (later combined with *Part I* of the series for publication) *Geom. Funct. Anal.* **31** (2021), 325-401.
9. *Two phase free boundary problem for Poisson kernels.* (with Simon Bortz, Max Engelstein, Max Goering, Tatiana Toro) *Indiana U. Math. J.* **71** no. 1 (2022), 251-306.
10. *Dirichlet energy-minimizers with analytic boundary.* (with Camillo De Lellis) *Indiana Univ. Math. J.* **72** (2023), 1367-1428.
11. *Dirichlet problem in domains with lower dimensional boundaries.* (with Joseph Feneuil, Svitlana Mayboroda) *Rev. Mat. Iberoam.* **37** (2021), 821-910.
12. *Square function estimates, BMO Dirichlet problem, and absolute continuity of harmonic measure on lower-dimensional sets.* (with Svitlana Mayboroda) *Anal. PDE* **12** (2019), no. 7, 1843-1890.
13. *Uniform rectifiability and elliptic operators satisfying a Carleson measure condition. Part I: the small constant case.* (with Steve Hofmann, José María Martell, Svitlana Mayboroda, Tatiana Toro) arXiv:1710.06157.
14. *Boundary rectifiability and elliptic operators with  $W^{1,1}$  coefficients.* (with Tatiana Toro) *Adv. Calc. Var.* **14** (2021), 37-62.
15. *BMO solvability and the  $A_\infty$  condition of the elliptic measure in uniform domains.* *J. Geom. Anal.* **28** (2018), no. 2, 866-908.

## INVITED TALKS

---

- Feb. 2024 Analysis seminar, Brown University
- Feb. 2024 Geometry seminar, Lehigh University
- Dec. 2023 Seminar at the Morningside Center of Mathematics, Chinese Academy of Sciences
- Jul. 2023 Workshop on *Applied and Computational Differential Geometry and Geometric PDEs*, Banff International Research Station (BIRS)
- Jun. 2023 Workshop on the *Regularity Theory for Free Boundary and Geometric Variational Problems III*, Leviso Italy
- Jun. 2023 Conference on *Harmonic Analysis, PDEs, and GMT*, dedicated to Prof. Luis Escauriaza, Bilbao Spain
- May. 2023 Analysis & PDE seminar, Stanford University

Apr. 2023 PDE & Analysis seminar, University of Kentucky

Mar. 2023 Applied analysis seminar, Louisiana State University

Jan. 2023 2023 Joint Mathematics Meetings, special session on *Recent Developments in Geometric Measure Theory*, Boston

Nov. 2022 Differential Geometry seminar, National Center for Theoretical Sciences in Taiwan

Oct. 2022 86th Midwest PDE seminar, University of Missouri in Columbia

Sep. 2022 Nonlinear Analysis Seminar, Rutgers University

Aug. 2022 Calculus of Variations workshop, Oberwolfach

May. 2022 CBMS Conference on *Analysis, Geometry, and PDEs in a Lower-Dimensional World*, Florida State University

May. 2022 Analysis & PDE seminar, Stanford University

Apr. 2022 2022 Joint Mathematics Meetings, special session on *Geometric Measure Theory*

Apr. 2022 Workshop on Geometric Measure Theory and Harmonic Analysis, Hausdorff Research Institute for Mathematics

Mar. 2022 AMS Spring Central Sectional Meeting, special session on *A Women in Analysis Research Network Event*

Mar. 2022 MSRI Hot Topics Workshop: *Regularity Theory for Minimal Surfaces and Mean Curvature Flow*

Feb. 2022 UK virtual harmonic analysis seminar

Feb. 2022 Analysis and Probability seminar, University of Connecticut

Dec. 2021 Analysis seminar, Yale University

Nov. 2021 Analysis and PDE seminar, MIT

Oct. 2021 Geometry and Analysis seminar, Columbia University

Oct. 2021 Center for Nonlinear Analysis seminar, Carnegie Mellon University

Oct. 2021 Analysis and Partial Differential Equations Seminar, Johns Hopkins University

Oct. 2021 Virtual analysis and PDE seminar (hosted by the University of California Irvine)

Oct. 2021 Fields Institute Geometric Analysis Colloquium, Toronto

Oct. 2021 Geometric Analysis and Applications seminar, Yale University

Sep. 2021 Workshop on the *Regularity Theory for Free Boundary and Geometric Variational Problems*, Levico Italy

Jun. 2021 Minisymposium in *Harmonic Analysis and PDE*, 8th European Congress of Mathematics, Slovenia

Jun. 2021 Analysis seminar, University of Warwick

May. 2021 Analysis & PDE seminar, Stanford University

Apr. 2021 Geometric Analysis seminar, University of California San Diego

Mar. 2021 PDE seminar, University of Minnesota

Dec. 2020 Rainwater seminar, University of Washington

- Oct. 2020 Virtual Maxwell Analysis Seminar, University of Edinburgh and Heriot-Watt University
- Sep. 2020 Mid-Atlantic Analysis Meeting seminar
- Aug. 2020 Analysis & PDE summer seminar, University of Minnesota
- Aug. 2020 Calculus of Variations workshop, Oberwolfach
- Jul. 2020 Analysis and PDE online seminar
- May. 2020 PDE CDT Lunchtime seminar, Center for Doctoral Training in PDEs, University of Oxford
- May. 2020 (cancelled due to COVID) Geometric analysis conference, Fordham University
- Jan. 2020 PDE seminar, Purdue University
- Nov. 2019 Calderón-Zygmund analysis seminar, University of Chicago
- Nov. 2019 2019 Prairie analysis seminar
- Jun. 2019 Harmonic analysis and PDEs conference, University of Helsinki
- Mar. 2019 AMS special session on *Topics at the Interface of Analysis and Geometry*, Honolulu HI
- Mar. 2019 AMS special session on *Interactions between GMT, PDE and Harmonic Analysis*, Honolulu HI
- Feb. 2019 IAS analysis seminar
- Feb. 2019 IAS mathematical conversations
- Dec. 2018 Princeton/IAS GMT seminar
- Nov. 2018 Analysis seminar, University of Pennsylvania
- Nov. 2018 AMS special session on *Harmonic Analysis and Partial Differential Equations*, Fayetteville, AR
- Sep. 2018 Harmonic analysis and PDE's seminar, CUNY Graduate Center
- Jul. 2018 Research program seminar, PCMI Harmonic Analysis program
- May. 2018 Rainwater seminar, University of Washington
- Apr. 2018 AMS special session on *Regularity of PDEs on Rough Domains*, Boston MA
- Apr. 2018 AMS special session on *Geometric Measure Theory and Partial Differential Equations*, Portland OR
- Sep. 2017 Seminario de análisis y aplicaciones, ICMAT Madrid
- Jun. 2017 S.I.G.M.A. seminar, University of Connecticut
- Jun. 2017 Analysis seminar, Nankai University
- Mar. 2017 Student harmonic analysis and PDE seminar, University of California, Berkeley
- Mar. 2017 Graduate student seminar at MSRI, Berkeley
- Sep. 2016 AMS special session on *Geometric Aspects of Harmonic Analysis*, Brunswick ME

## INVITED MINI-COURSES

---

- Mini-course on *Almgren's regularity of area-minimizing currents and multi-valued functions*, workshop on *Geometric measure theory and applications*, University College London, Jul. 25-27, 2022
- Mini-course on the *Quantitative unique continuation of elliptic PDEs*, workshop on the *Free boundary problems and related topics*, ETH Zurich, Jul. 4-8, 2022

## CONFERENCE REPORTS, SURVEYS, ETC.

---

- *Quantitative boundary unique continuation and the estimate of the singular set* (extended abstract), Oberwolfach Reports No. 37 (2022), <https://publications.mfo.de/handle/mfo/3976>
- *Boundary regularity of area-minimizing currents: a linear model with analytic interface* (extended abstract), Oberwolfach Reports No. 22 (2020), <https://publications.mfo.de/handle/mfo/3792>

## PROFESSIONAL ACTIVITIES & SERVICE

---

- Jul. 2023 - **Graduate committee**, Johns Hopkins University
- Apr. 2023 **Speaker** at the *Path Through Math* event organized by the UChicago's Society of Women in Math (SWiM)
- Dec. 2022 **Co-organizer** of a session on *Harmonic functions and Laplace eigenfunctions* at the 2022 Pacific Rim Mathematical Association Congress, Vancouver, Canada
- Summer 2021 Mentoring an undergraduate reading project on the topic of geometric measure theory, student: Oliver Thakar (Princeton University)
- Oct. 2020 – **Co-organizer** of the Calderón-Zygmund analysis seminar, University of Chicago
- May. 2023
- Jul. 2020 Taught a **mini-course** (virtually) at the University of Chicago summer REU
- Jan. 2020 **Co-organizer** of JMM session on *Interfaces between PDEs and geometric measure theory*, Denver CO
- Nov. 2019 – **Committee member** at the departmental EDI (Equity, Diversity and Inclusion) committee, University of Chicago
- Feb. 2021
- May. 2019 **Teaching assistant** at the Women and Mathematics program *Topics in geometric analysis*, Institute for Advanced Study
- Held regular review sessions to support the *Terng lecture series* given by Prof. T. Toro.
- 2018 – **Referee** for multiple journals, including Adv. Math., Arch. Rational Mech. Anal., Commun. Part. Diff. Eq., Comm.Pure Appl.Math., Duke Math. J., Geom. Funct. Anal., Int. Math. Res. Notices, J. Geom. Anal., J. London Math. Soc., Mem. Am. Math. Soc., etc.
- Apr. 2019 **Co-organizer** of AMS special session on *Regularity Theory of PDEs and Calculus of Variations on Domains with Rough Boundaries*, Hartford CT

- Jul. 2018      **Teaching assistant** at the PCMI Graduate Summer School, Park City UT  
 – Held regular problem sessions to support the lectures by Prof. S. Hofmann.
- Summer 2018    Co-organizer of preparatory sessions for graduate students' **prelim/qualification exam** on *Real analysis*, University of Washington
- May. 2018      **Panelist** at the panel on academic job market, University of Washington
- 2015 - 2016    **Co-organizer** of Graduate Student Analysis Seminar, University of Washington
- 2012            Student analysis seminar, École Normale Supérieure

## GRANTS, HONORS & AWARDS

---

- 2019-2023    NSF Postdoctoral Research Fellowship, Award #1902756
- May. 2020    (postponed due to COVID) London Mathematical Society's *Visiting speakers to the UK*, hosted by Prof. N. Wickramasekera at the University of Cambridge (one month)
- 2018            College of Arts and Sciences *Graduate Medalist* in Natural Sciences, University of Washington  
 – annual award to one graduating student in each of the divisions of *Humanities, Natural Sciences* and *Social Sciences*
- Sep. 2017    Tanzi-Egerton Fellowship, University of Washington
- Sep. 2015    Academic Excellence Award, University of Washington
- 2013-2016    Microsoft Scholar Award, University of Washington
- 2011-2013    Sophie Germain International Master scholarship, Jacques Mathematics Foundation (FMJH)
- 2010            Academic Innovation Award, Peking University

## SELECTED TEACHING EXPERIENCES

---

- Autumn 2023    **Instructor** of *Real Analysis*, Johns Hopkins University  
 – first-year graduate course in real analysis
- Autumn 2022    **Instructor** of IBL-style *Honors Calculus*, University of Chicago  
 Winter 2023
- Autumn 2020    **Instructor** of *Honors Calculus*, in hybrid form (in-person and virtual), University of Chicago  
 Winter 2021  
 – IBL (Inquiry-based learning) style for highly selective first-year undergraduate students, with a strong emphasis on students presentations and class discussions
- July 2020      **Instructor** of a mini-course on *Harmonic measures*, University of Chicago summer REU

Summer 2018 **Instructor** of *Introduction to Differential Equations*, University of Washington  
 Autumn 2017 **Grader** for *Complex Analysis*, University of Washington  
 Autumn 2016 **Instructor** of *Introduction to Differential Equations*, University of Washington  
 Autumn 2015 **Grader** for *Fundamental Concepts of Analysis*, University of Washington  
 Spring 2015 **TA** for *Calculus with Analytic Geometry III*, University of Washington  
 Winter 2014 **TA** for *Application of Calculus to Business and Economics*, University of Washington  
 – calculus class for students majoring in business and economics, where we focus more on problem-solving techniques with applications in economics and finance  
 Spring 2014 **TA** for *Calculus with Analytic Geometry II*, University of Washington

## CONFERENCES & WORKSHOPS ATTENDED

---

- Oberwolfach workshop on Partial Differential Equations, Jul. 23-28, 2023
- Joint Northwestern-UChicago Geometric Analysis Seminar, Apr. 22, 2023
- Zhentong Chern-Weil symposium, University of Chicago, Oct. 7-9, 2022
- Summer school on *Geometric analysis and calibrated geometries*, ETH Zurich, Jun. 13-17, 2022
- *Geometric Measure Theory and its Applications*, a conference on the occasion of Bob Hardt's retirement, Rice University, Mar. 17-20, 2022
- Trimester program on the *Interactions between Geometric measure theory, Singular integrals, and PDE*, Hausdorff Research Institute for Mathematics, Bonn, Jan. 10 - Apr. 22, 2022
- *Geometric measure theory and applications*, Cortona (Italy), Palazzone SNS, Aug. 30 - Sep. 3, 2021
- FRG *New Challenges in GMT*, University of Washington, Seattle, Aug. 24 - Sep. 4, 2020
- Oberwolfach workshop on the *Calculus of Variations*, Aug. 2-8, 2020
- *The 27th Southern California geometric analysis seminar*, University of California, Irvine, Feb. 8-9, 2020
- Workshop on *Illustrating Geometry and Topology*, ICERM, Brown University, Sep. 16-20, 2019
- *Geometric measure theory and applications: from geometric analysis to free boundary problems*, Cetraro (Italy), Sep. 2-6, 2019
- Nonlinear PDEs discussion group at Courant Institute, Apr. 19, 2019
- Workshop on *Variational methods in geometry*, IAS, Nov. 5-9, 2018 and Mar. 4-8, 2019
- Allen-Cahn/Ginzburg-Landau reading group, IAS, Sep.-Dec. 2018
- PCMI Summer Session on harmonic analysis, Park City, Jul. 1-21, 2018

- *Harmonic analysis and geometric measure theory*, conference in honor of Guy David, CIRM Marseille, Oct. 2-6, 2017
- *Recent developments in harmonic analysis* workshop, MSRI, May. 15-19, 2017
- *Harmonic analysis and elliptic equations on real Euclidean spaces and on rough sets*, MSRI summer graduate school, Jun. 13-24, 2016
- Introductory workshop: *Randomness and long-time dynamics in nonlinear evolution differential equations*, MSRI, Aug. 24-28, 2015
- *Reflectionless measures, Wolff's potentials and rectifiability*, NSF-CBMS Regional Conference in the Mathematical Sciences, North Dakota State University, Jul. 27-31, 2015
- Workshop for women in analysis and PDE, Institute for Mathematics and its Applications, May. 28-31, 2015
- The eighteenth Rivière-Fabes symposium on Analysis and PDE & Spring 2015 Midwest PDE conference, University of Minnesota, Apr. 17-19, 2015
- *Uniqueness in analysis and geometry*, Massachusetts Institute of Technology, Dec. 10-11, 2014
- *Harmonic analysis and PDEs recent developments and future directions*, conference in honor of Carlos Kenig, University of Chicago, Sep. 19-21, 2014
- *Dispersive partial differential equations*, MSRI summer graduate school, Jun. 16-27, 2014
- International conference on nonlinear PDEs and satellite workshop *Free surface & interface problems*, University of Oxford, Sep. 10-15, 2012
- *Inverse problems and partial differential equations* summer school, University of Washington, Jul. 2-20, 2012
- Hadamard lectures on *Error estimates in stochastic homogenization* by Prof. Felix Otto, University of Paris-Sud XI, Mar.-Apr. 2012