

MATH 126 D  
Exam II  
November 22, 2011

Name \_\_\_\_\_

Student ID # \_\_\_\_\_

Section \_\_\_\_\_

HONOR STATEMENT

“I affirm that my work upholds the highest standards of honesty and academic integrity at the University of Washington, and that I have neither given nor received any unauthorized assistance on this exam.”

SIGNATURE: \_\_\_\_\_

1	12	
2	13	
3	12	
4	12	
Total	50	

- Your exam should consist of this cover sheet, followed by 4 problems. Check that you have a complete exam.
- Show all work and justify your answers.
- Unless otherwise indicated, your answers should be exact values rather than decimal approximations. (For example,  $\frac{\pi}{4}$  is an exact answer and is preferable to its decimal approximation 0.7854.)
- You may use a scientific calculator and one 8.5×11-inch sheet of handwritten notes. All other electronic devices (including graphing calculators) are forbidden.
- The use of headphones or earbuds during the exam is not permitted.
- There are multiple versions of the exam, you have signed an honor statement, and cheating is a hassle for everyone involved. DO NOT CHEAT.
- Turn your cell phone OFF and put it AWAY for the duration of the exam.

GOOD LUCK!

1. (12 points) Let  $\vec{r}(t) = \langle \sin 3t, \ln(\sin 3t), \cos 3t \rangle$  for  $0 < t < \frac{\pi}{3}$ .

(a) Find the unit tangent, unit normal, and binormal vectors at  $t = \frac{\pi}{6}$ .

ANSWERS:

$$\vec{T}\left(\frac{\pi}{6}\right) = \underline{\hspace{2cm}} \quad \vec{N}\left(\frac{\pi}{6}\right) = \underline{\hspace{2cm}} \quad \vec{B}\left(\frac{\pi}{6}\right) = \underline{\hspace{2cm}}$$

(b) Give the equation of the normal plane to  $\vec{r}(t)$  at  $t = \frac{\pi}{6}$ .

2. (13 points) Find the point(s) on the surface  $x^2 = 12 + yz$  closest to the point  $(0, 1, 3)$ . For full credit you must show some work OR write a sentence or two to explain how you know that your answer gives the minimal distance.

3. (12 points)

(a) Calculate the iterated integral.

$$\int_0^4 \int_0^2 xy\sqrt{x^2+1} dx dy.$$

(b) Sketch the region of integration and change the order of integration.

$$\int_0^{10} \int_0^{x^2+1} h(x,y) dy dx.$$

4. (12 points) Compute the area of the region **to the right of the  $y$ -axis**, outside the circle  $r = \sin(\theta)$ , and inside the cardioid  $r = 1 + \sin(\theta)$ .

