DIFFERENTIAL GEOMETRY/PDE SEMINAR

Friday, February 1, 2008 Padelford C-401 2:30-3:20 pm

Optimal Regularity and Free Boundary Structure of Signorini or Thin Obstacle Problems

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The problem of minimizing the Dirichlet integral, or more general integrals which correspond to second order operators, in domain Ω in \mathbb{R}^3 among all functions with prescribed boundary values f(x) and constrained to remain above a prescribed obstacle $\varphi(x)$ when restricted to (n-1)-manifold M in Ω is known as the thin obstacle problem or the n-dimensional Signorini problem.

When studying the regularity of the solution the best that one expects to attain is a $C^{1,1/2}$ on each side of the manifold M even with a smooth $\varphi(x)$. This is indeed the case as it was shown by D. Richardson in 1978 for n = 2 and M a hyperplane, for higher dimensions, i.e. when $n \geq 3$, only a $C^{1,\alpha}$ had been achieved for some $0 < \alpha \leq 1/2$ by L. A. Caffarelli (1979).

In a 2004 joint work with L. A. Caffarelli we show that 1/2 can be obtained for any dimension by making use of the almost concavity of u in the normal direction and considering a monotonicity formula of an appropriate quantity.

This opened the way to study the properties of the interface by using geometric P.D.E. techniques. This is precisely the content of a recent joint work with L. A. Caffarelli and S. Salsa. We show there that there is one basic global non-degenerate profile after blow-up, and that in a neighborhood of a point which has this profile the free boundary is a $C^{1,\alpha}$ curve on the boundary i.e. a n-2 dimensional graph on the n-1 dimensional boundary. For more information about this seminar, visit the DG/PDE Seminar Web page (from the Math Department home page, www.math.washington.edu, follow the link Seminars, Colloquia, and Conferences).

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